

Centre of gravity of a body is defined as the point through which the whole weight of the body acts. A body can have only one centre of gravity for all portions of the body. It is represented by C.G or G.

Centroid -

The point at which the total area of a plane is assumed to be concentrated, is called the centroid of that area. It is also represented by G or C.G.

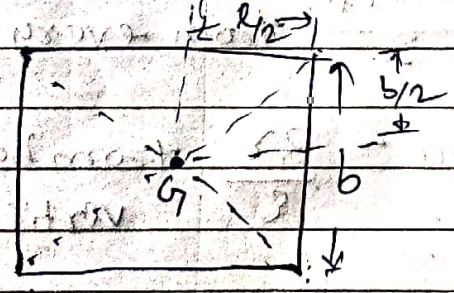
→ The centroid and centre of gravity are at the same point.

\* Methods for centre of gravity

- ① By geometrical considerations
- ② by moments
- ③ By graphical method.

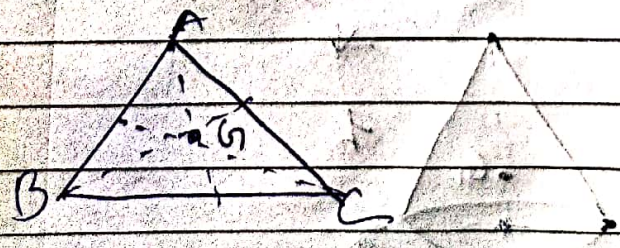
Centre of gravity or centroid of some plane fig

Rectangle / parallelogram



$G = (l/2, b/2)$  at the intersection of diagonals

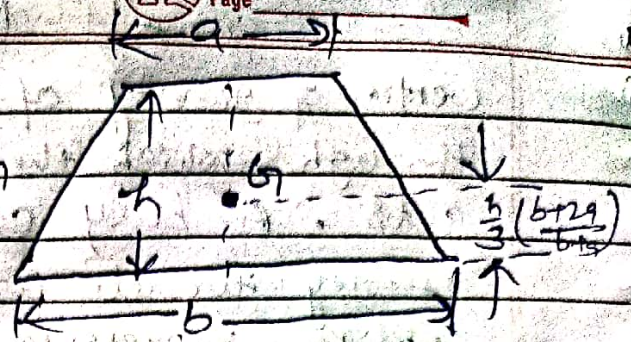
Triangle → At the intersection of medians.



Trapezium:

$G = \frac{h}{3} \left( \frac{b+2a}{b+a} \right)$  from base

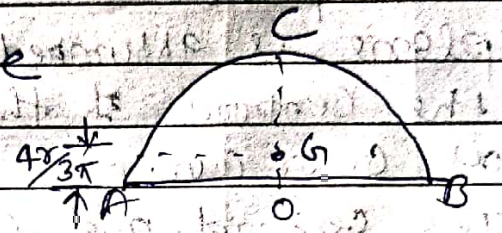
side b



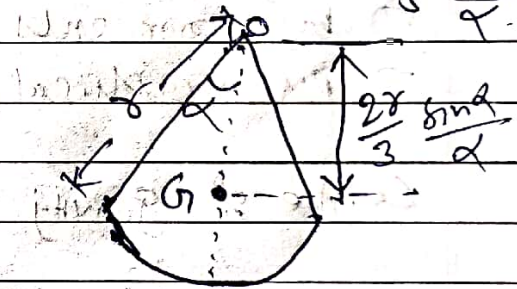
Semi-circle:

$G = \frac{4r}{3\pi}$  from base

measured along vertical radius



Circular sector: - C.G. of ~~semi~~ circular sector of semi-vertical angle  $\alpha$  is at a distance  $\frac{2r}{3} \frac{\sin \alpha}{\alpha}$

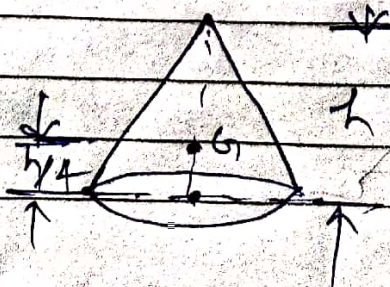


→ C.G. of cube =  $\frac{\text{side}}{2}$  from every face.

→ C.G. of sphere =  $\frac{\text{diameter}}{2}$  from every point.

→ C.G. of hemisphere =  $\frac{3r}{8}$  from base along vertical radius.

→ C.G. of right circular solid cone is at distance of  $\frac{h}{4}$  from its base along vertical axis.



# Centre of gravity by moments

$$M\bar{x} = m_1x_1 + m_2x_2 + m_3x_3 + \dots$$

$$\therefore \bar{x} = \frac{\sum m \cdot x}{M}$$

$$\bar{y} = \frac{\sum m \cdot y}{M}$$

M = total moments

M =  $m_1 + m_2 + \dots$

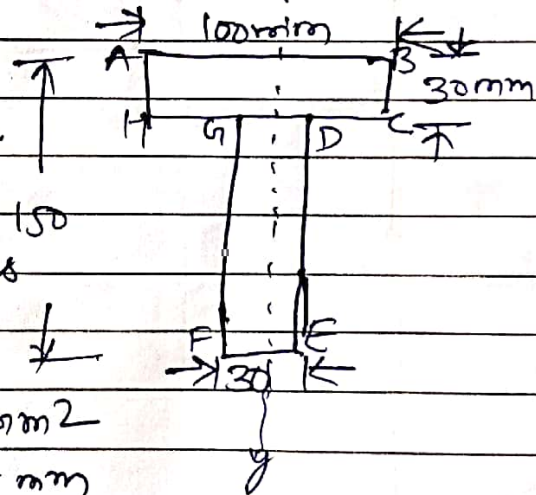
For plane figures it has only Area not mass.

$$\bar{x} = \frac{a_1x_1 + a_2x_2 + \dots}{a_1 + a_2 + a_3 + \dots}$$

$$\bar{y} = \frac{a_1y_1 + a_2y_2 + \dots}{a_1 + a_2 + a_3 + \dots}$$

Example → find centre of gravity of a 100mm x 150mm x 30mm T-section.

Section is symmetrical about y-y axis. therefore its C.G. lies on this axis.



Let FE be the reference axis

Rectangle ABCD

$$a_1 = 100 \times 30 = 3000 \text{ mm}^2$$

$$y_1 = (150 - \frac{30}{2}) = 135 \text{ mm}$$

Rectangle DEFG

$$a_2 = 120 \times 30 = 3600 \text{ mm}^2, y_2 = \frac{120}{2} = 60 \text{ mm}$$

$$\bar{y} = \frac{a_1y_1 + a_2y_2}{a_1 + a_2} = \frac{3000 \times 135 + 3600 \times 60}{3000 + 3600} \text{ mm}$$

$\bar{y} = 94.1 \text{ mm}$  from FE on the y-y axis.